

Warm Up:  
Solve the following:

$$\frac{15}{x} = \frac{2.5}{7}$$

$$\begin{array}{l} 105 = 2.5x \\ \frac{105}{2.5} = \frac{2.5x}{2.5} \\ x = 42 \end{array}$$

$$\frac{y}{12} = \frac{77}{84}$$

$$84y =$$

Because percents can be expressed as ratios, you can use the proportion

$$\frac{\text{percent}}{100} = \frac{\text{part}}{\text{whole}}$$

to solve percent problems.

Just use the above formula for solving word problems. The percent stays a whole number and think what is the whole group and what is the percentage group?

**A poll taken one day before an election showed that 22.5% of voters planned to vote for a certain candidate. If 1800 voters participated in the poll, how many indicated that they planned to vote for that candidate?**

$$\frac{\%}{100} = \frac{\text{Part}}{\text{Whole}}$$

$$\frac{22.5}{100} \times \frac{x}{1800}$$

$$\frac{100x}{100} = \frac{40500}{100}$$

$$x = 405$$

**At Clay High School, 434 students, or 35% of the students, play a sport. How many students does Clay High School have?**

$$\frac{35}{100} \times \frac{434}{x}$$

$$\frac{35x}{35} = \frac{43400}{35}$$

$$x = 1240$$

A **rate** is a ratio that involves two different units. You are familiar with many rates, such as miles per hour (mi/h), words per minute (wpm), or dollars per gallon of gasoline. Rates can be helpful in solving many problems.

**Ryan ran 600 meters and counted 482 strides. How long is Ryan's stride in inches?**  
(*Hint: 1 m  $\approx$  39.37 in.*)

$$\frac{600}{482} = 1.24 \text{ in}$$

$$1.24 \cdot 39.37 \\ = 48.81 \text{ in}$$

**Luis ran 400 meters in 297 strides. Find his stride length in inches.**

$$1\text{m} = 39.37\text{in}$$

$$\frac{400}{297} = 1.35 \text{ m} \cdot 39.37\text{in}$$

$$= 53.02\text{in}$$

I need a volunteer. This room is 9 meters long.

E1:

Volunteer walk from back white board to front. How many strides?

12.5

What is their stride length in inches?

$$1\text{m} = 39.37\text{in}$$

$$\frac{9}{12.5} = .72 \cdot 39.37 =$$

*Similar* figures have the same shape but not necessarily the same size. Two figures are **similar** if their corresponding angles are congruent and corresponding sides are proportional.

You can use knowledge from Geometry to find similar figure lengths. To solve these problems:

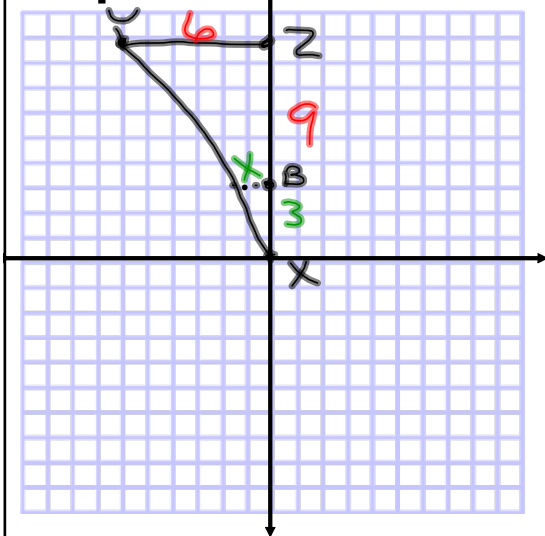
- 1) Graph what you are given
- 2) Set up a proportion to find missing side lengths.

$$\frac{\Delta 1}{\Delta 2} = \frac{\Delta 1}{\Delta 2}$$

$\Delta XYZ$  has vertices  $X(0, 0)$ ,  $Y(-6, 9)$  and  $Z(0, 9)$ .

$\Delta XAB$  is similar to  $\Delta XYZ$  with a vertex at  $B(0, 3)$ .

Graph  $\Delta XYZ$  and  $\Delta XAB$  on the same grid.



$$\frac{\Delta 1}{\Delta 2} = \frac{\Delta 1}{\Delta 2}$$

$$\frac{x}{6} = \frac{3}{9}$$

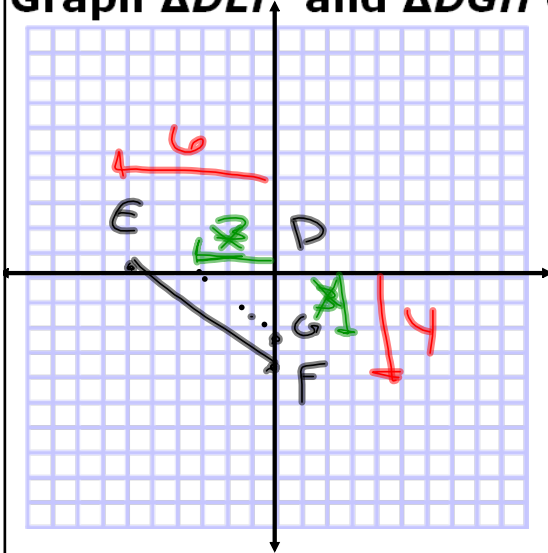
$$9x = 18$$

$$x = 2$$

$\triangle DEF$  has vertices  $D(0, 0)$ ,  $E(-6, 0)$  and  $F(0, -4)$ .

$\triangle DGH$  is similar to  $\triangle DEF$  with a vertex at  $G(-3, 0)$ .

Graph  $\triangle DEF$  and  $\triangle DGH$  on the same grid.



$$\frac{3}{6} = \frac{x}{4}$$

$$12 = 6x$$

$$x = 2$$

You can also estimate heights and lengths using similar triangles. To solve these problems:

- 1) Draw a picture (it helps to see)
- 2) Set up a proportion using similar sides and solve.

The tree in front of Luka's house casts a 6-foot shadow at the same time as the house casts a 22-foot shadow. If the tree is 9 feet tall, how tall is the house?



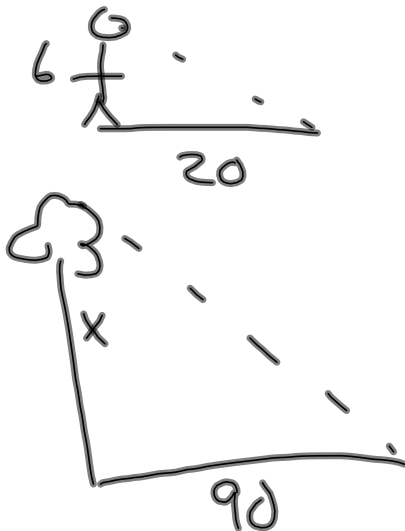
$$\frac{\Delta 1}{\Delta 2} = \frac{\Delta 1}{\Delta 2}$$

$$\frac{9}{x} = \frac{6}{22}$$

$$\frac{6x}{6} = \frac{198}{6}$$

$$x = 33 \text{ ft}$$

A 6-foot-tall climber casts a 20-foot long shadow at the same time that a tree casts a 90-foot long shadow. How tall is the tree?



$$\frac{6}{x} = \frac{20}{90}$$

$$540 = 20x$$

$$x = 27$$

## 2-3 Graphing Linear Functions

### *Objectives*

Determine whether a function is linear.

Graph a linear function given two points, a table, an equation, or a point and a slope.



## 2-3 Graphing Linear Functions

### *Vocabulary*

linear function

slope

y-intercept

x-intercept

slope-intercept form





Functions that are linear have a constant change, also known as a constant slope. To find if a table is linear:

- 1) Find the differences between consecutive  $x$  and  $y$  values.
- 2) Is the difference of  $y$  divided by the difference of  $x$  the same for all?

**Determine whether the data set could represent a linear function.**

$x$	-2	0	2	4
$f(x)$	2	1	0	-1

+2      +2      +2

-1      -1      -1

Linear

Determine whether the data set could represent a linear function.

<b>x</b>	2	3	4	5
<b>f(x)</b>	2	4	8	16

+1   +1   +1  
+2   +4   +8

Not  
Linear

Determine whether the data set could represent a linear function.

<b>x</b>	4	11	18	25
<b>f(x)</b>	-6	-15	-24	-33

+7   +7   +7  
-9   -9   -9

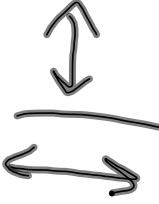
**Determine whether the data set could represent a linear function.**

<b><math>x</math></b>	<b>10</b>	<b>8</b>	<b>6</b>	<b>4</b>
<b><math>f(x)</math></b>	<b>7</b>	<b>5</b>	<b>1</b>	<b>-7</b>

The slope of a linear function is the constant ratio of  $y$  divided by  $x$ , also known as...

$$-\frac{1}{4} \rightarrow -\frac{1}{4}$$

$\frac{\text{rise}}{\text{run}}$

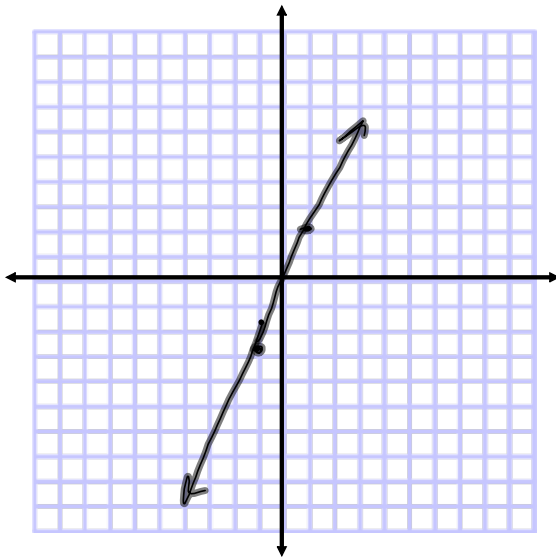


To graph with a point and slope:

- 1) Plot point.
- 2) Use slope to plot more points and connect. The top number is your rise (up/down), the bottom number is run (left/right)

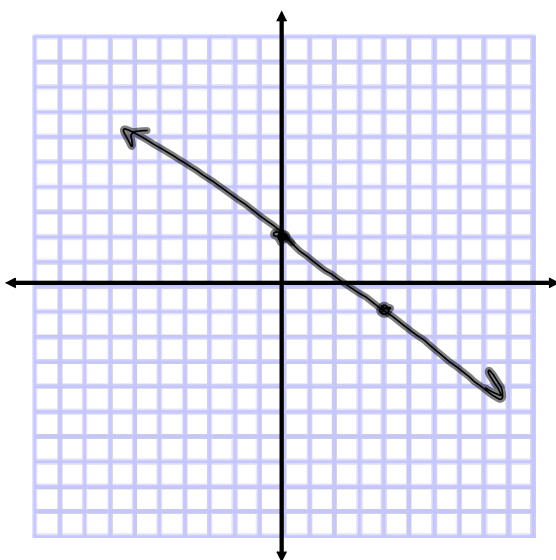
Graph the line with slope  $\frac{5}{2}$  that passes through  $(-1, -3)$ .

$$\begin{array}{l} \frac{5}{2} \rightarrow \uparrow 5 \\ \quad \rightarrow \rightarrow 2 \end{array}$$

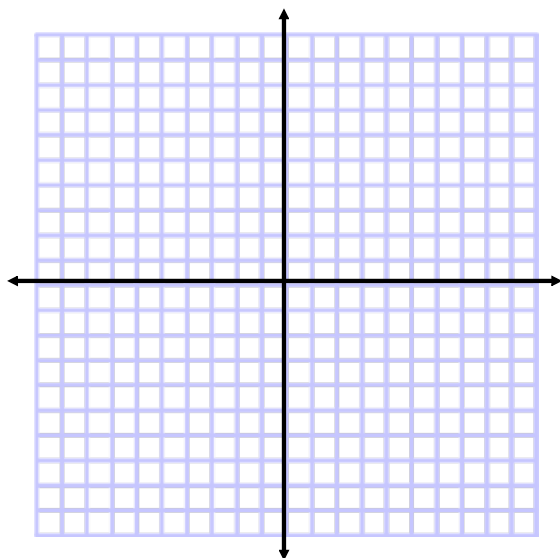


Graph the line with slope  $-\frac{3}{4}$  that passes through  $(0, 2)$ .

$$\begin{array}{l} -\frac{3}{4} \rightarrow \downarrow 3 \\ \quad \rightarrow \rightarrow 4 \end{array}$$

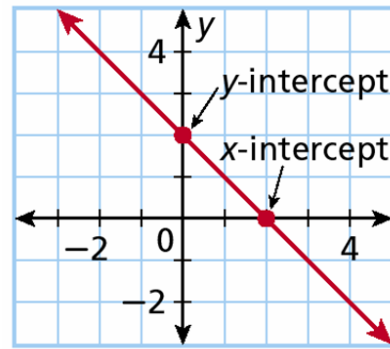


**Graph the line with slope  $\frac{4}{3}$  that passes through  $(3, 1)$ .**



Choose a point. Choose a slope. Now graph it.

The **y-intercept** is the  $y$ -coordinate of a point where the line crosses the  $x$ -axis.

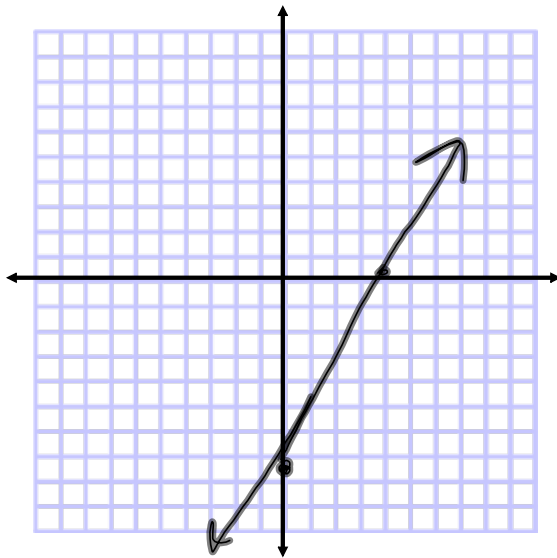


The **x-intercept** is the  $x$ -coordinate of a point where the line crosses the  $y$ -axis.

To find the intercepts:

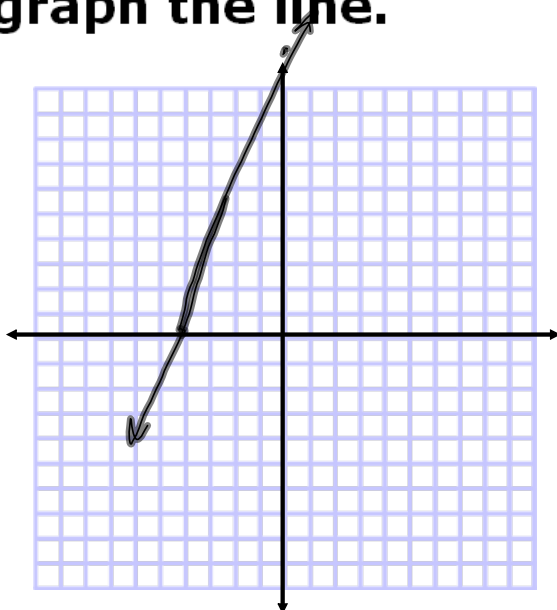
- 1) To find  $x$ -intercept: Plug in 0 for  $y$ , and solve for  $x$
- 2) To find  $y$ -intercept: Plug in 0 for  $x$ , and solve for  $y$ .

Find the intercepts of  $4x - 2y = 16$ , and graph the line.



y-int:	x-int:
$4 \cdot 0 - 2y = 16$	$4x - 2 \cdot 0 = 16$
$-2y = 16$	$4x = 16$
$y = -8$	$x = 4$
$(0, -8)$	$(4, 0)$

Find the intercepts of  $6x - 2y = -24$ , and graph the line.



x-int:	y-int:
$6x = -24$	$-2y = -24$
$x = -4$	$y = 12$

Write your own equation.  
Find the intercepts.

Linear functions can also be expressed as linear equations of the form  $y = mx + b$ . When a linear function is written in the form  $y = mx + b$ , the function is said to be in **slope-intercept form** because  $m$  is the slope of the graph and  $b$  is the  $y$ -intercept. Notice that slope-intercept form is the equation solved for  $y$ .

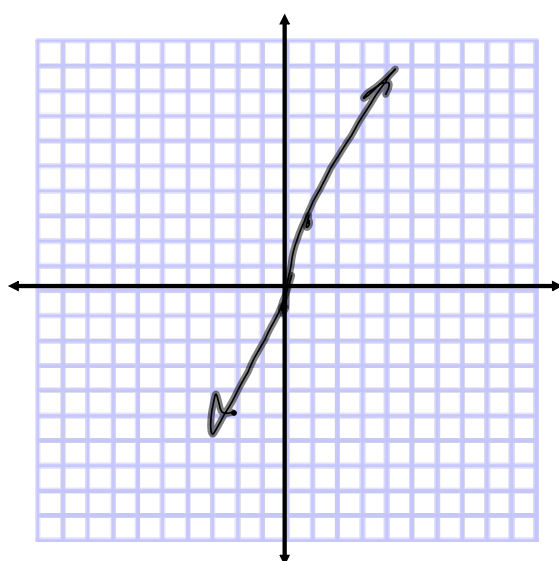
$m \rightarrow$  Slope  
 $b \rightarrow$   $y$ -intercept



To write in slope-intercept form:

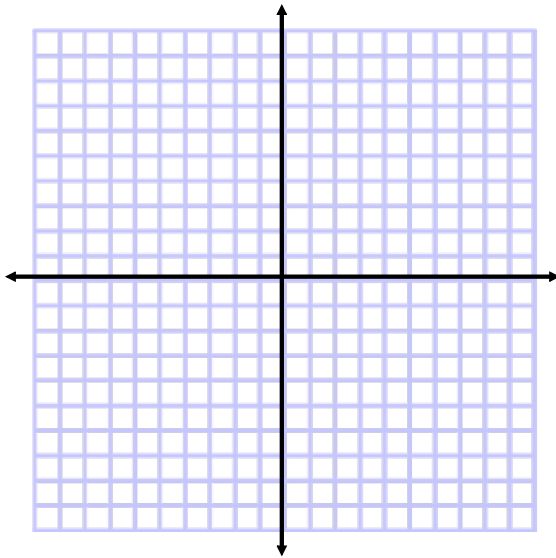
1) Solve for  $y$  to get  $y = \underline{\hspace{1cm}}x + \underline{\hspace{1cm}}$

**Write the function  $-4x + y = -1$  in slope-intercept form. Then graph the function.**

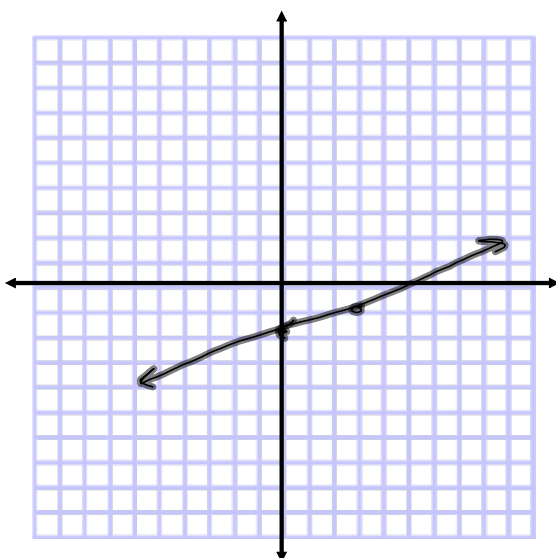


$$\begin{aligned} -4x + y &= -1 \\ +4x \quad +4x & \\ y &= 4x - 1 \end{aligned}$$

Write the function  $x + \frac{3}{4}y = 6$  in slope-intercept form. Then graph the function.



Write the function  $5x = 15y + 30$  in slope-intercept form. Then graph the function.



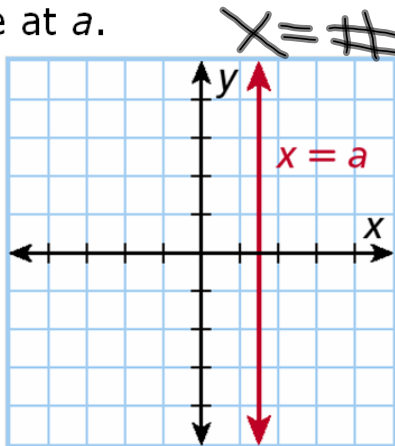
$$y = \frac{1}{3}x - 2$$

## 2-3 Graphing Linear Functions

### Vertical and Horizontal Lines

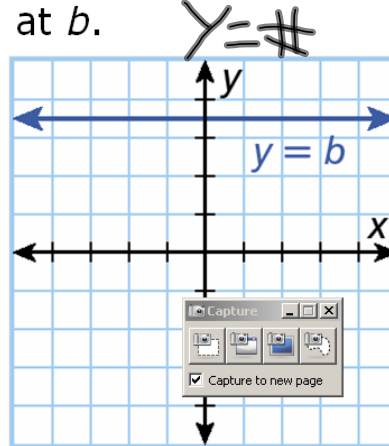
#### Vertical Lines

The line  $x = a$  is a vertical line at  $a$ .



#### Horizontal Lines

The line  $y = b$  is a horizontal line at  $b$ .



## 2-3 Graphing Linear Functions

### Example 5: Graphing Vertical and Horizontal Lines

Determine if each line is vertical or horizontal.

A.  $x = 2$

Vert

B.  $y = -4$

Horz

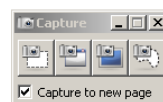


**2-3 Graphing Linear Functions****Check It Out! Example 5**

Determine if each line is vertical or horizontal.

A.  $y = -5$

B.  $x = 0.5$



Homework:

p. 101 #18-21, 30, 33

p. 110 # 22-38 (evens), 50, 52

Present: p.101 #33

p.110 #50