

Warm up:

Given the function $y = 3^x$

Translate the function to the left 2 units and down 4 units. What is the new function?

$$y = 3^{x+2} - 4$$

Given the function $y = \log 4x$

Translate 7 units up and reflect over the x-axis. What is the new function?

$$y = -\log 4x + 7$$

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Curve Fitting with Exponential and Logarithmic Models

Objectives

Model data by using exponential and logarithmic functions.

Use exponential and logarithmic models to analyze and predict.

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Vocabulary

exponential regression
logarithmic regression

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Analyzing data values can identify a pattern, or repeated relationship, between two quantities.

Look at this table of values for the exponential function $f(x) = 2(3^x)$.

x	-1	0	1	2	3
$f(x)$	$\frac{2}{3}$	2	6	18	54

$\times 3 \quad \times 3 \quad \times 3 \quad \times 3$

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Notice that the *ratio* of each y -value and the previous one is constant. Each value is three times the one before it, so the ratio of function values is constant for equally spaced x -values. This data can be fit by an exponential function of the form $f(x) = ab^x$.

If a set of values has a second difference that continues to climb each time that is when we have found an exponential relationship. If it becomes constant on the second difference then it is just quadratic.

$$\frac{24}{16} = \frac{3}{2}$$

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Example 1: Identifying Exponential Data

Determine whether f is an exponential function of x of the form $f(x) = ab^x$. If so, find the constant ratio.

A.

x	-1	0	1	2	3
$f(x)$	2	3	5	8	12

B.

x	-1	0	1	2	3
$f(x)$	16	24	36	54	81

Quadratic
2nd difference
is constant

+1 +2 +3 +4

First Differences

+8 +12 +18 +27

$$\frac{81}{54} = \frac{54}{36} = \frac{36}{24} = \frac{24}{16}$$

Exponential

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Check It Out! Example 1

Determine whether y is an exponential function of x of the form $f(x) = ab^x$. If so, find the constant ratio.

a.

x	-1	0	1	2	3
$f(x)$	2.6	4	6	9	13.5

1.32 3 4.5
1.6 1 1.5
Exponential
 $\frac{6}{4} = \frac{3}{2}$

b.

x	-1	0	1	2	3
$f(x)$	-3	2	7	12	17

5 5 5 5
0 0 0
 $-\frac{2}{3} \neq \frac{7}{2}$ Linear

You have worked with regressions before by finding linear and quadratic regressions. You can also find exponential regressions. The calculator will find the best equation fulfilling the equation $y = ab^x$

To find an exponential regression:

- Plug your points into 2 set lists
- Choose for your calculator to find an exp reg

$$\frac{L_1}{x} \quad \frac{L_2}{y}$$

exp Reg

To predict a value:

- 1) Put your regression equation into the y1 column
- 2) Put the number they want predicted in the y2 column
- 3) Graph them both and find the intersection. The x-value will be your prediction.

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Remember!

If you do not see r^2 and r when you calculate regression, **2nd** CATALOG **0** and turn these on by selecting **DiagnosticOn**.

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Example 2: College Application

Find an exponential model for the data. Use the model to predict when the tuition at U.T. Austin will be \$6000.

Tuition of the University of Texas	
Year	Tuition
1999-00	\$3128
2000-01	\$3585
2001-02	\$3776
2002-03	\$3950
2003-04	\$4188

$$y_1 = 3022.75(1.07)^x$$

$$y_2 = 6000$$

$$(10.13, 6000)$$

2009-2010

1
2
3
4
5
L₁ L₂

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Check It Out! Example 2

Use exponential regression to find a function that models this data. When will the number of bacteria reach 2000?

Time (min)	0	1	2	3	4	5
Bacteria	200	248	312	390	489	610

$$y_1 = 199.29(1.25)^x$$

$$y_2 = 2000$$

10.3

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Many natural phenomena can be modeled by natural log functions. You can use a **logarithmic regression** to find a function

Helpful Hint

Most calculators that perform logarithmic regression use \ln rather than \log .

You have the same steps to finding a logarithmic regression. One thing to remember is that the calculator will actually produce the equation using a NATURAL LOG (\ln), so just be aware of that.

~~log .723~~
Ln Reg ln .723

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Example 3: Application

Find a natural log model for the data. According to the model, when will the global population exceed 9,000,000,000?

$$y = 1824 + 106.48 \ln x$$

2057

Global Population Growth	
Population (billions)	Year
1	1800
2	1927
3	1960
4	1974
5	1987
6	1999

X
L₁ ~~X~~ Y
L₂ L₂

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Check It Out! Example 4

Use logarithmic regression to find a function that models this data. When will the speed reach 8.0 m/s?

Time (min)	1	2	3	4	5	6	7
Speed (m/s)	0.5	2.5	3.5	4.3	4.9	5.3	5.6

$$y_1 = .587 + 2.638 \ln x$$

$$y_2 = 8$$

16.6 min

Homework:

p. 548 #8-13, 17, 24, 29

Present 13 and 24